

Thermal conductivity of Si-Ge-based nanostructures

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GEFÖRDERT VOM

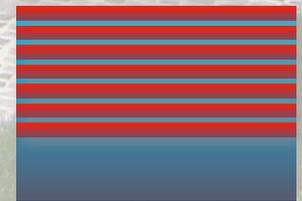


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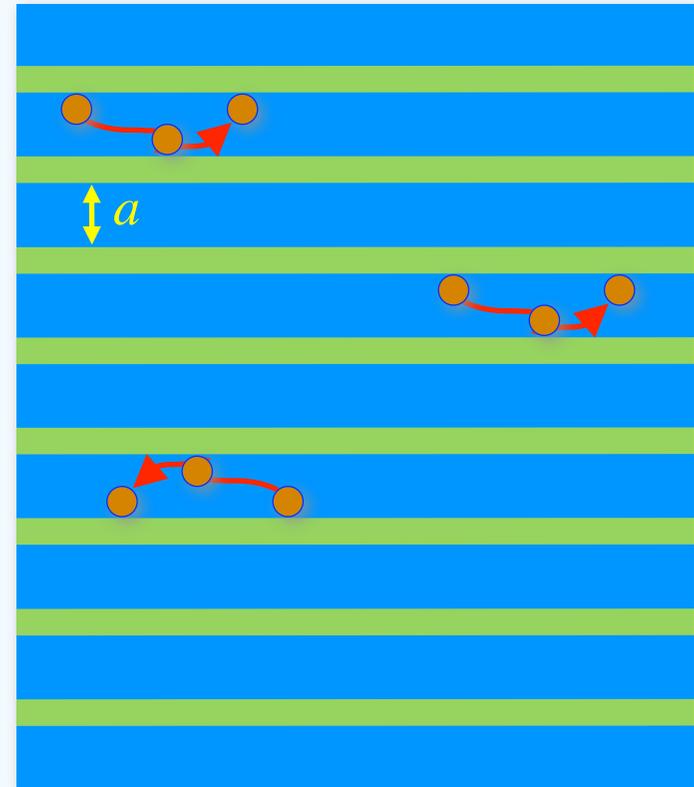


Reduction in thermal conductivity

Cross-plane transport in SL → Coherent phonon scattering at interfaces

$$\kappa_{\text{ph}} = \frac{1}{3} C v \ell$$

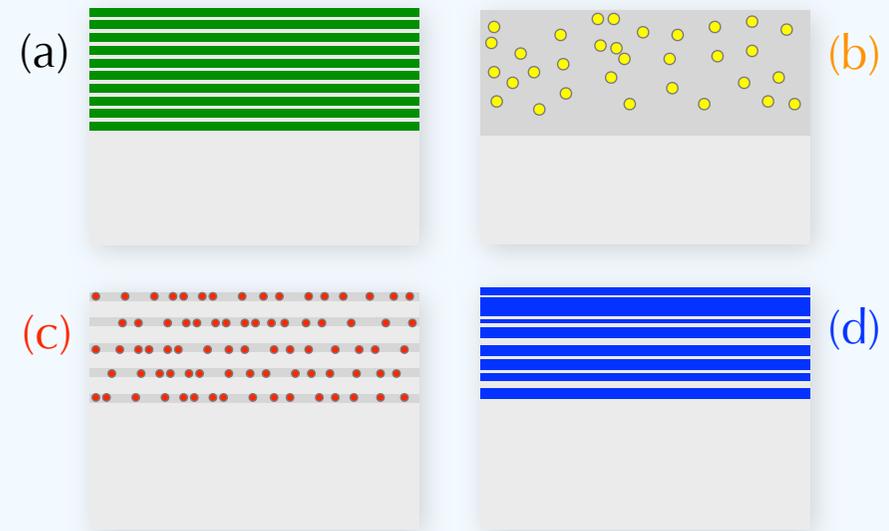
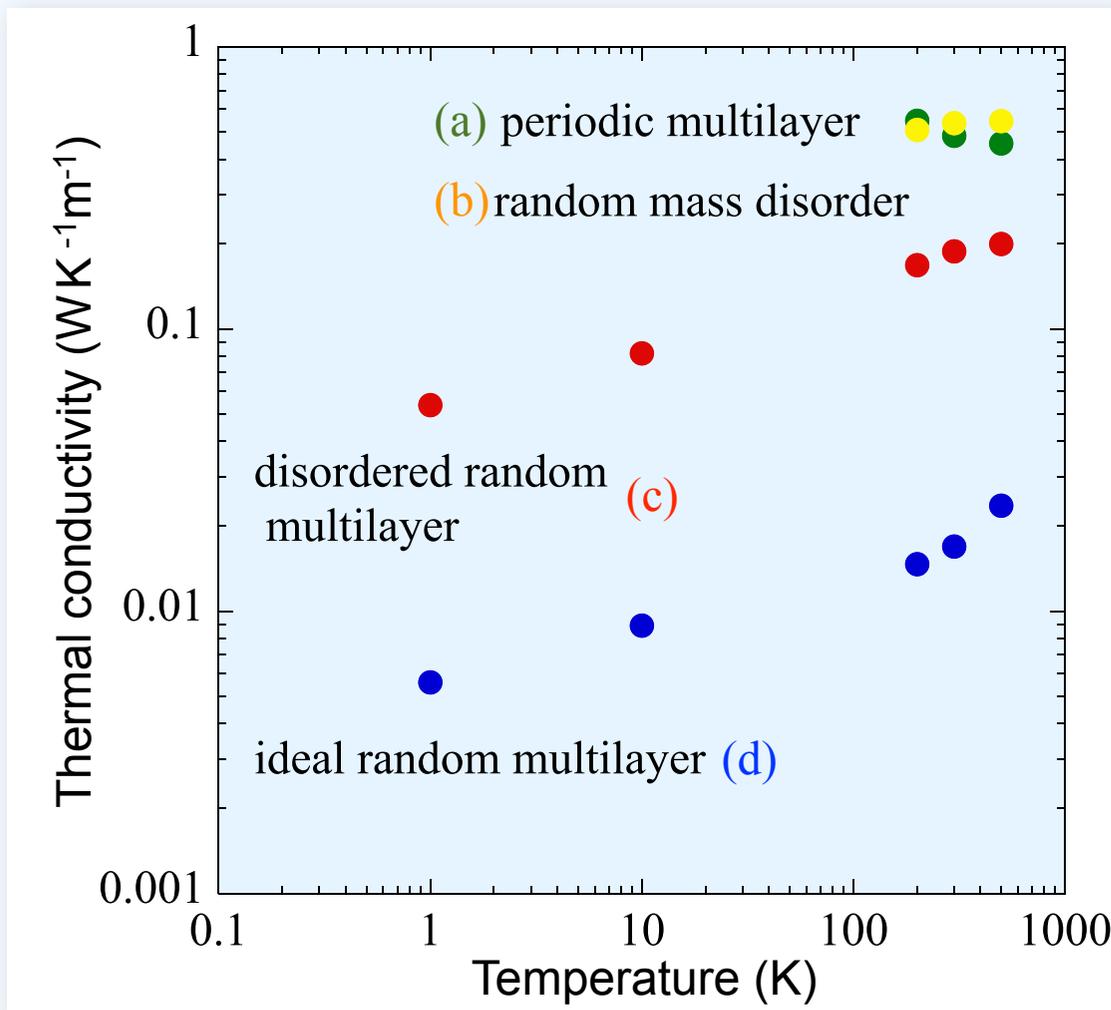
(C lattice heat capacity, v speed of sound,
 ℓ mean free path of phonons)



If layer thickness $a < \ell$, the thermal conductivity of the lattice κ_{ph} is reduced.

Phonon scattering

Superlattices, composites, quantum dot SLs, random multilayers



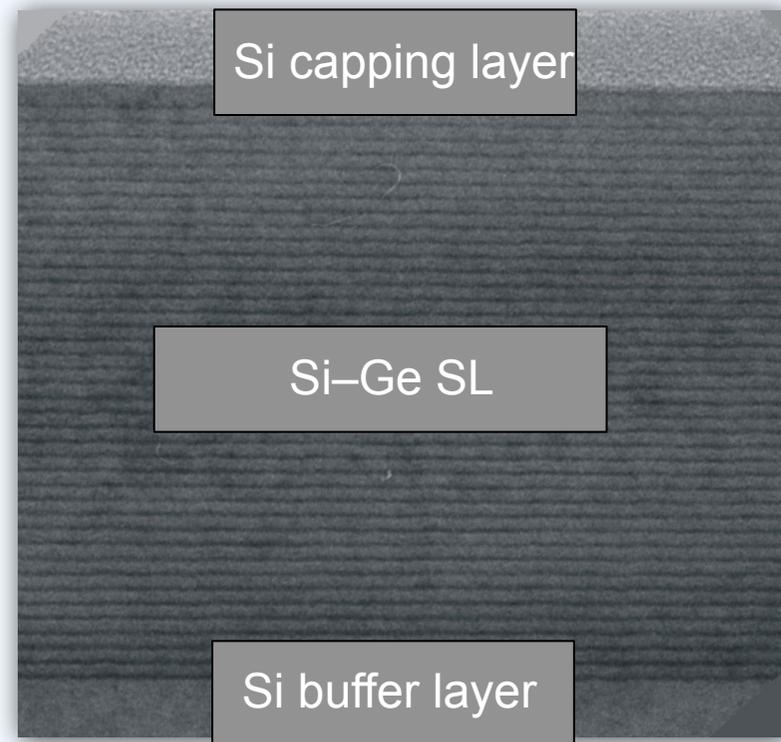
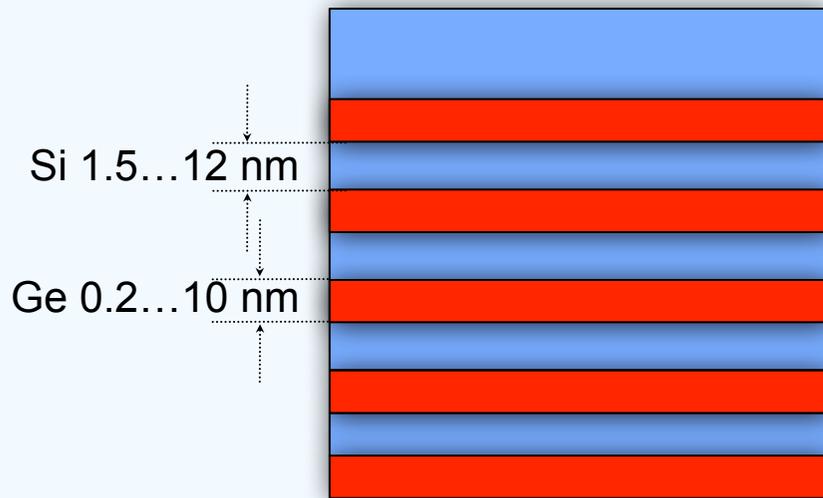
Anderson localization of phonons
in **nonperiodic structures**

MD Simulation

[Frachioni, White: J Appl Phys **112** (2012) 14320]

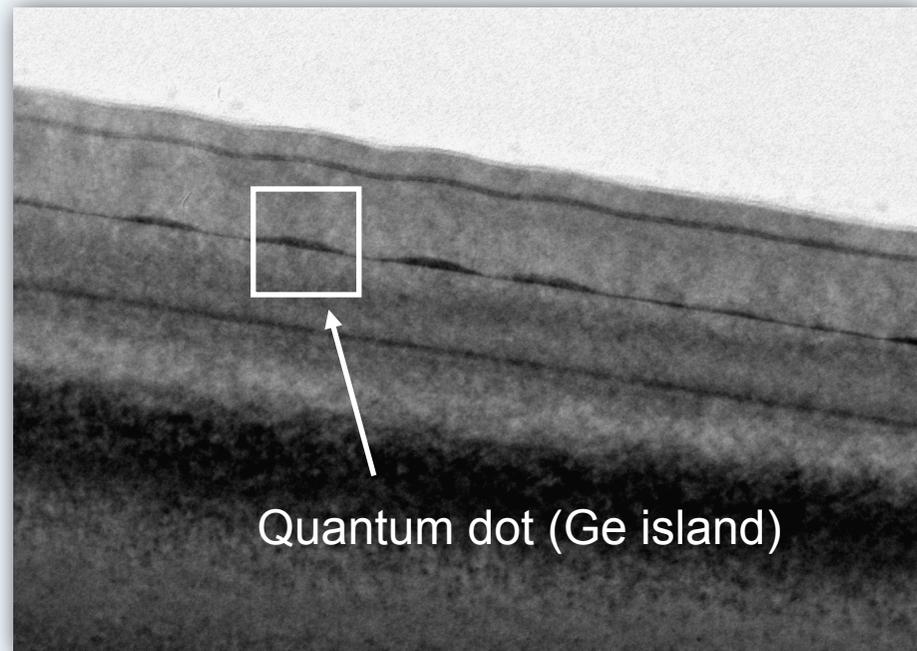
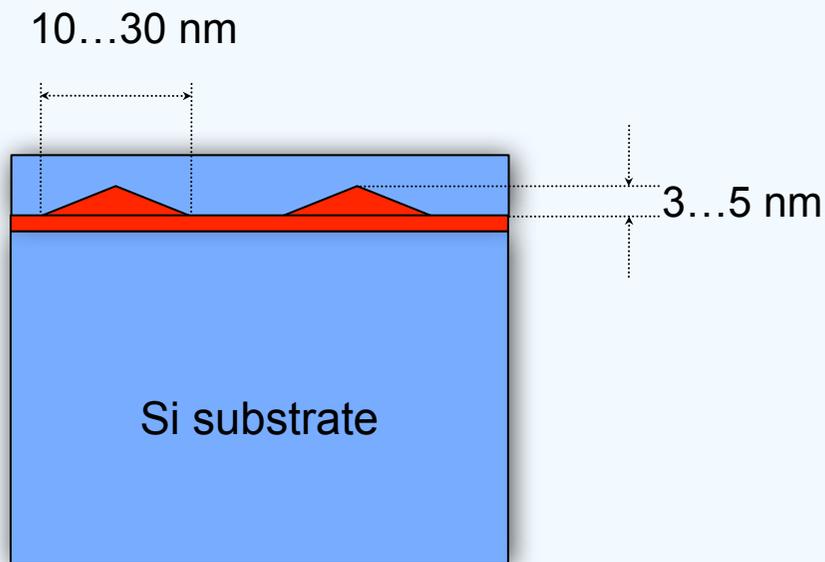
MBE of Si-Ge layers

- ◆ Stack of alternating layers of Si and a $\text{Si}_{1-x}\text{Ge}_x$ alloy
- ◆ Precision of single layers: ± 0.2 nm



Quantum dot Si-Ge superlattice

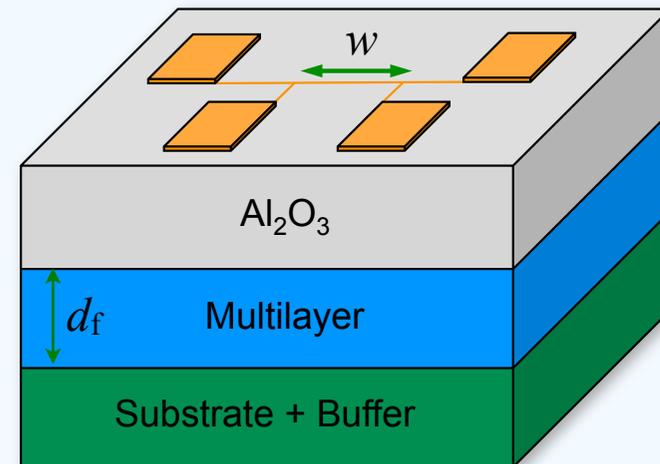
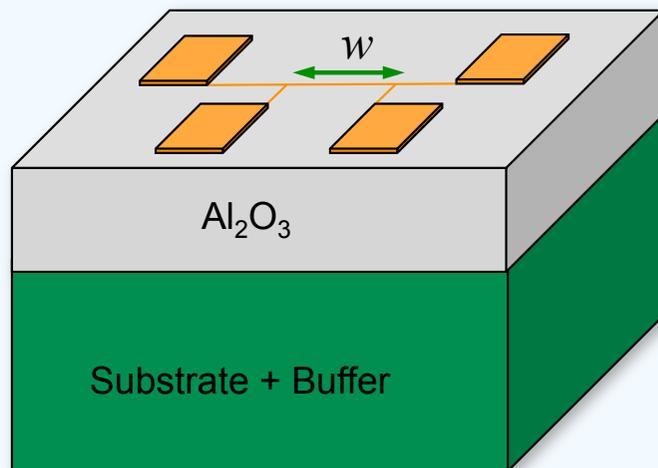
- ◆ (001), (111) orientation of the Si substrate
- ◆ Si (111) → flat layers
- ◆ Si (100) → Ge islands (density $\sim 10^9 \dots 10^{11} \text{ cm}^{-2}$)



100 nm

3ω measurements

- ◆ Deposition of a 100 nm insulating Al_2O_3 layer by ALD
- ◆ Reference sample without the multilayer structure
- ◆ Differential 3ω measurement of the thermal conductivity of thin films, $U_{3\omega} = f(\kappa)$



Thin film thermal conductivity

1D heat flow

Measurement with one bolometer stripe, width $2b \gg d_f$

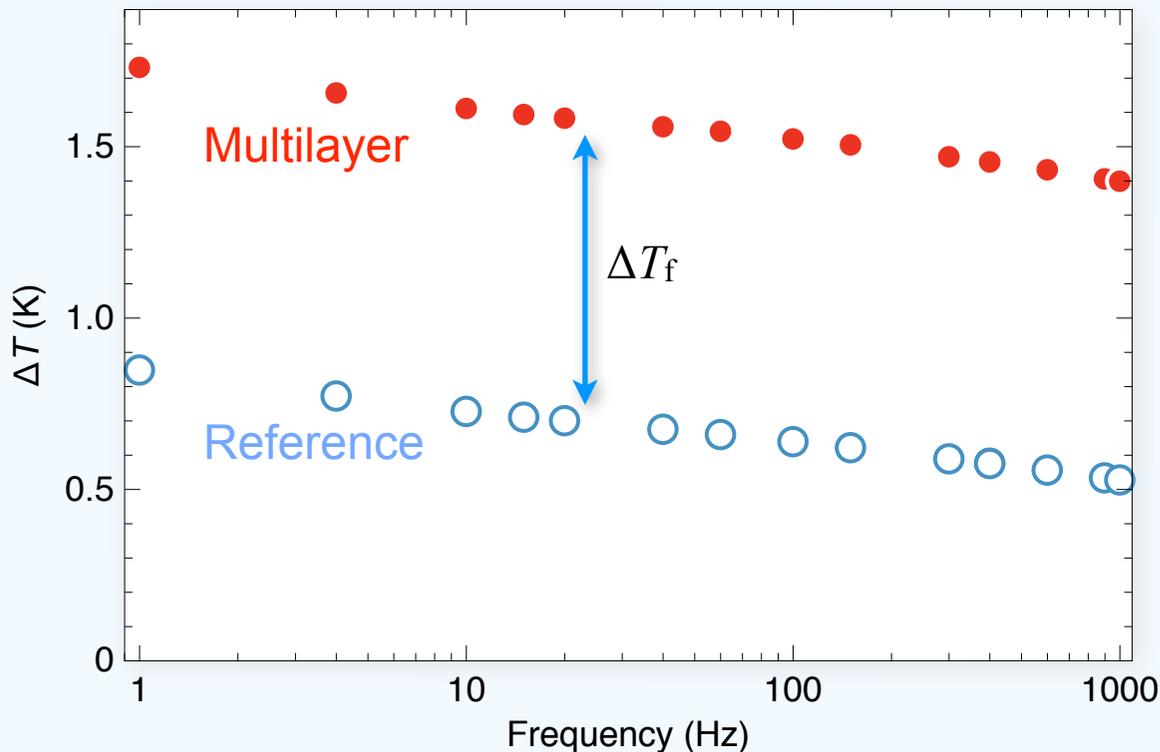
$\Delta T_f \rightarrow$ 1D thermal conductivity κ_{1D}

2D heat flow

Measurements with two bolometer stripes, b_1 and b_2

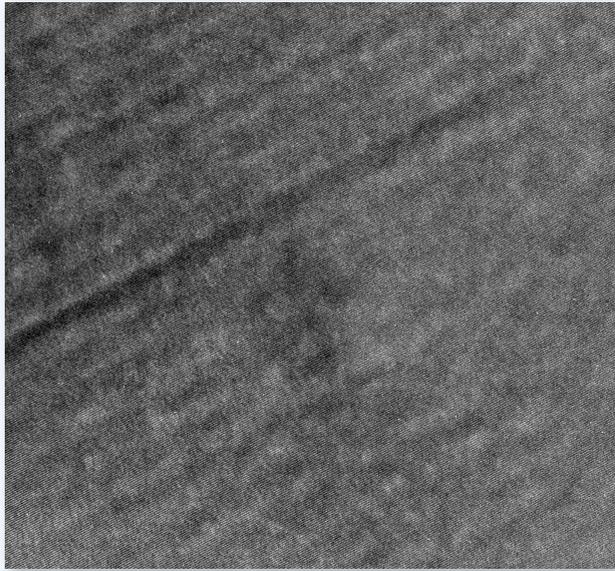
$\Delta T_f \rightarrow$ in-plane thermal conductivity κ_{\parallel}

\rightarrow cross-plane thermal conductivity κ_{\perp}



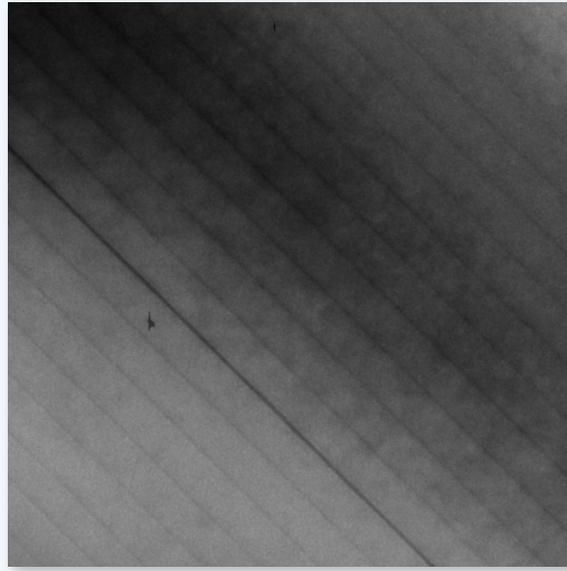
Bolometric temperature increase ΔT measured in a multilayer and a reference sample as a function of the frequency

Superlattices



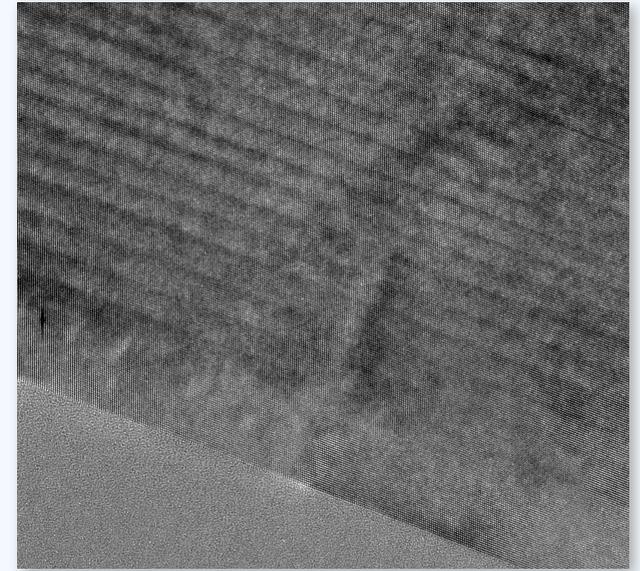
10 nm

0.2 nm Ge + 3.3 nm Si
171 \times , \approx 600 nm



50 nm

1.6 nm Ge + 12 nm Si
39 \times , \approx 600 nm



10 nm

2 nm Ge + 1.5 nm Si
171 \times , \approx 600 nm

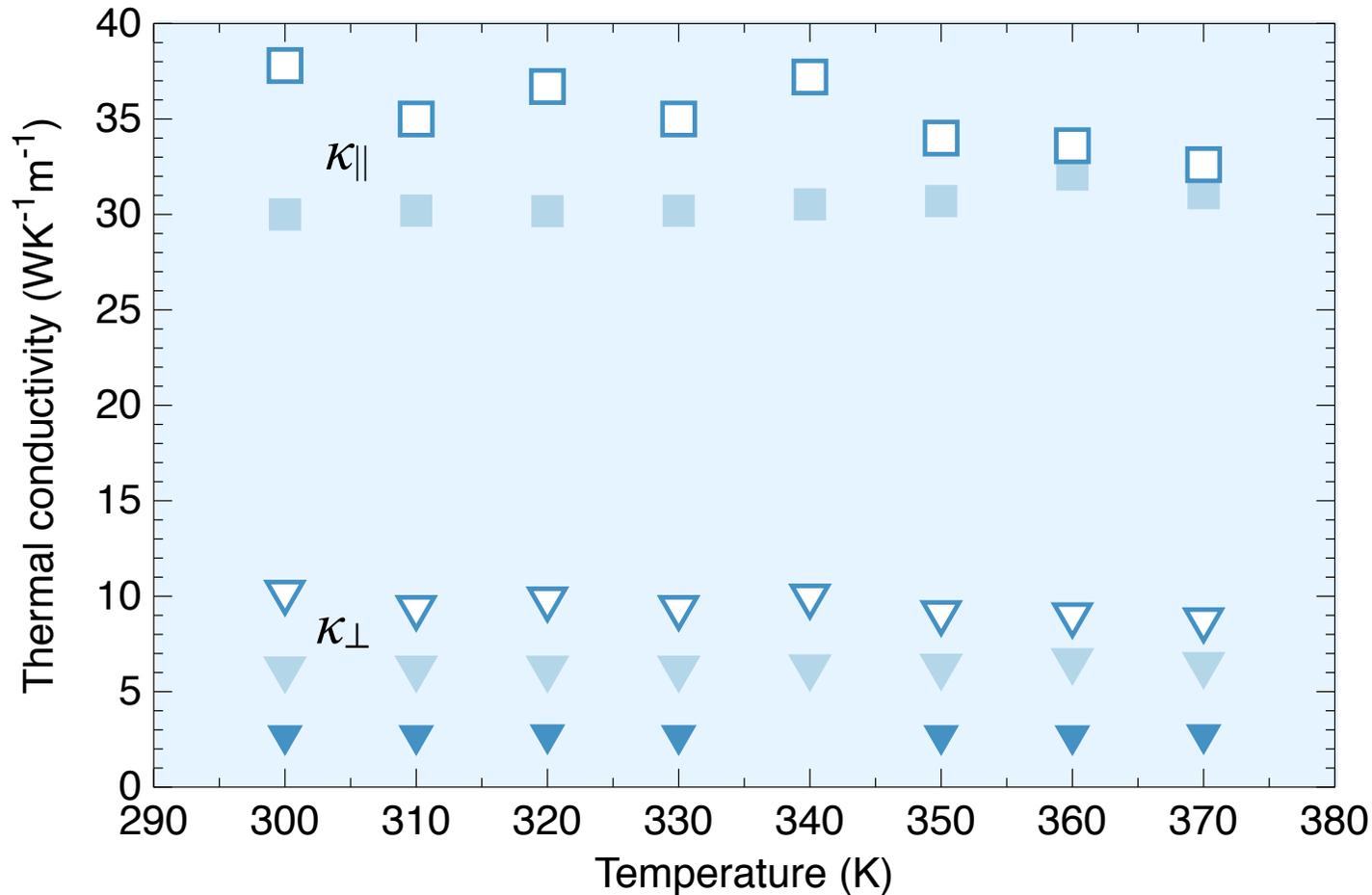
Ge content

1.7 %

3.5 %

17 %

Thermal conductivity of periodic SL



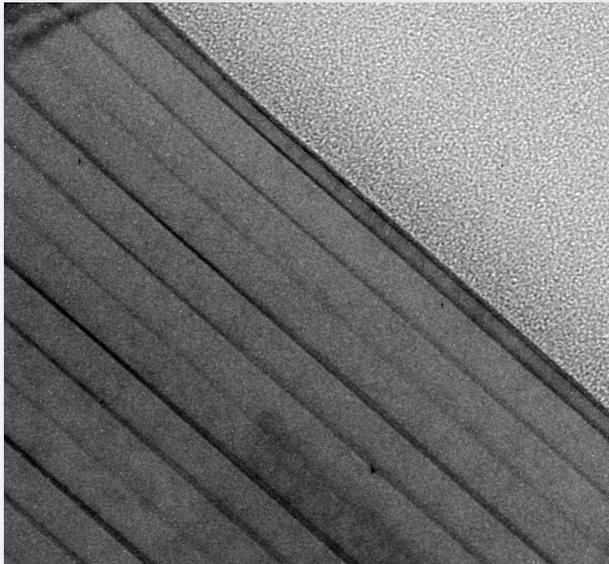
3.5 % Ge, period 13.6 nm
1.7 % Ge, period 4.5 nm

3.5 % Ge, period 13.6 nm
1.7 % Ge, period 4.5 nm
17 % Ge, period 4.5 nm

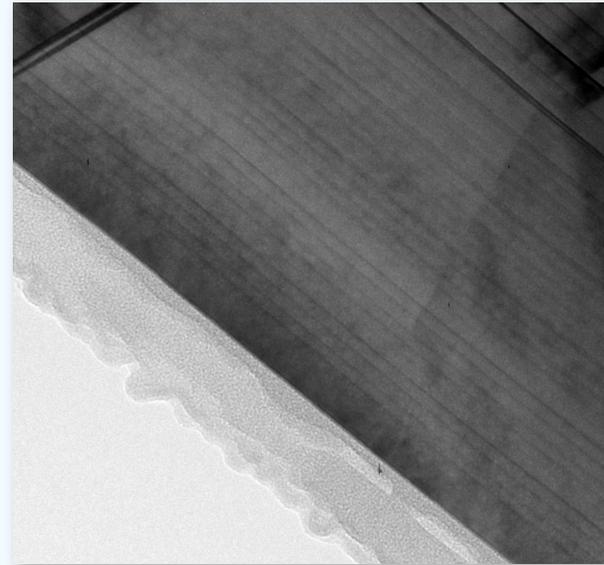
In-plane and cross-plane thermal conductivities for SLs
with different Ge contents and periods

Random multilayers

20 nm



1.2 nm Ge + 12 nm Si
1.2 nm Ge + 12 nm Si
1.8 nm Ge + 12 nm Si
0.9 nm Ge + 12 nm Si
1.6 nm Ge + 12 nm Si
6x, \approx 600 nm



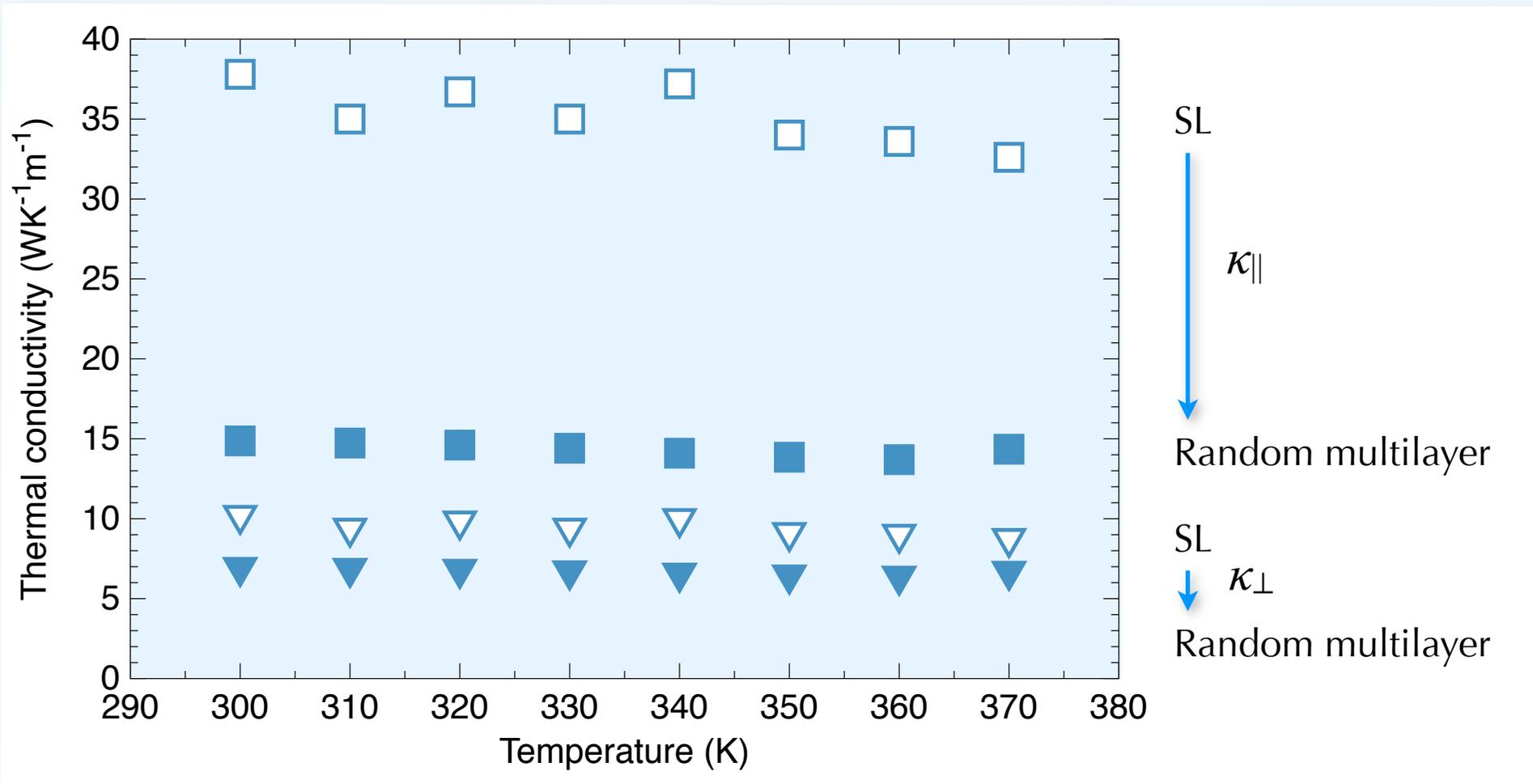
0.6 nm Ge + 4.1 nm Si
0.3 nm Ge + 5.1 nm Si
0.8 nm Ge + 4.8 nm Si
0.6 nm Ge + 5.7 nm Si
0.6 nm Ge + 3.8 nm Si
34x, \approx 940 nm

Ge content

2.9 %

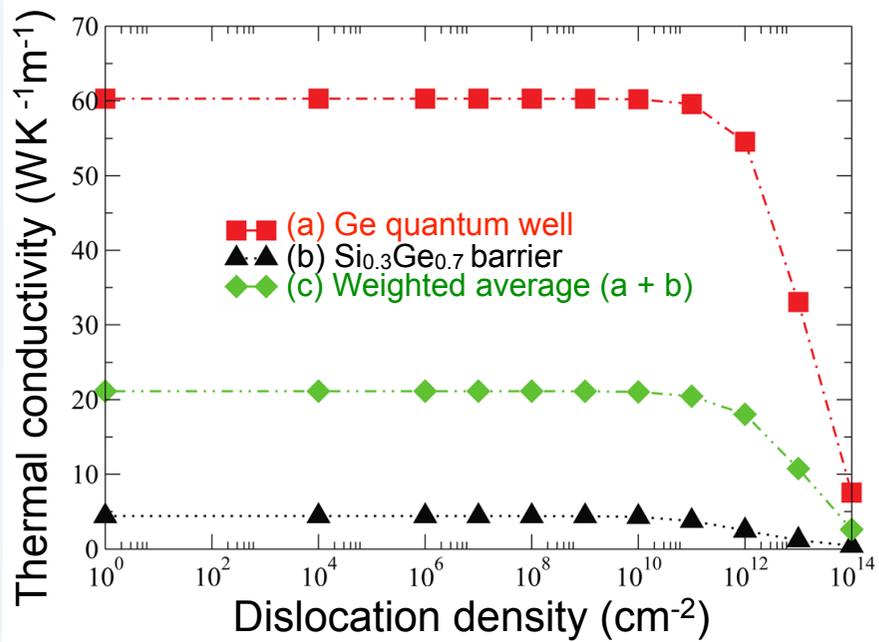
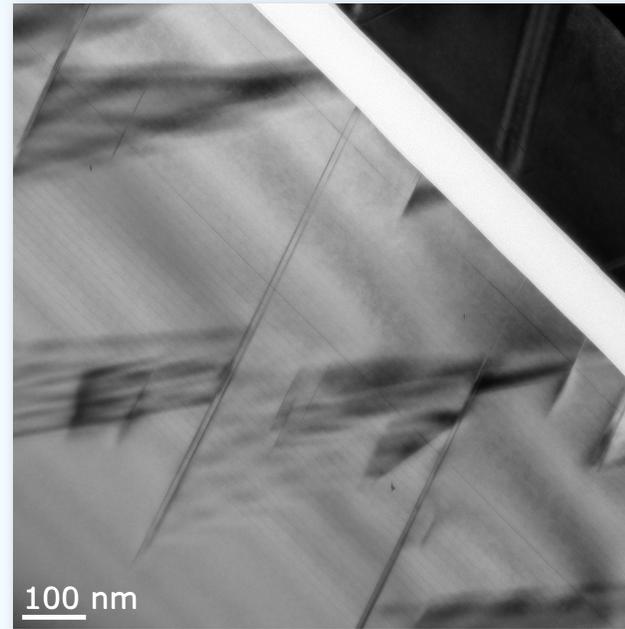
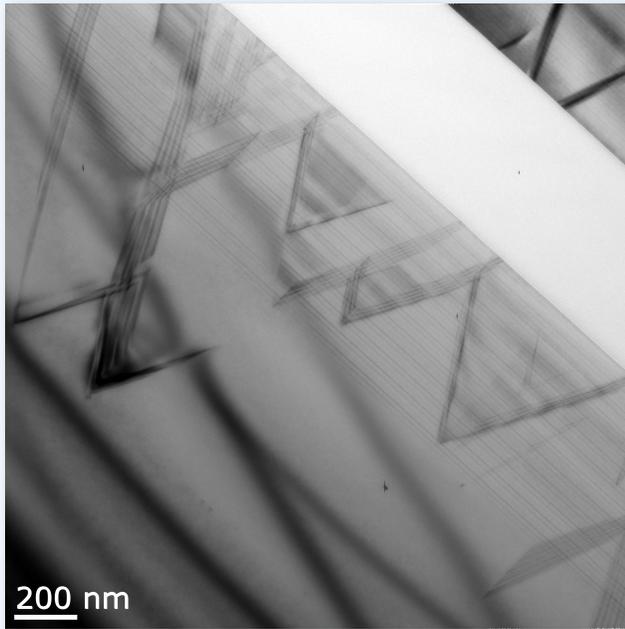
3.3 %

Results of random multilayers



Thermal conductivities in a random multilayer (2.9 % Ge)
in comparison to a superlattice(3.5 % Ge).

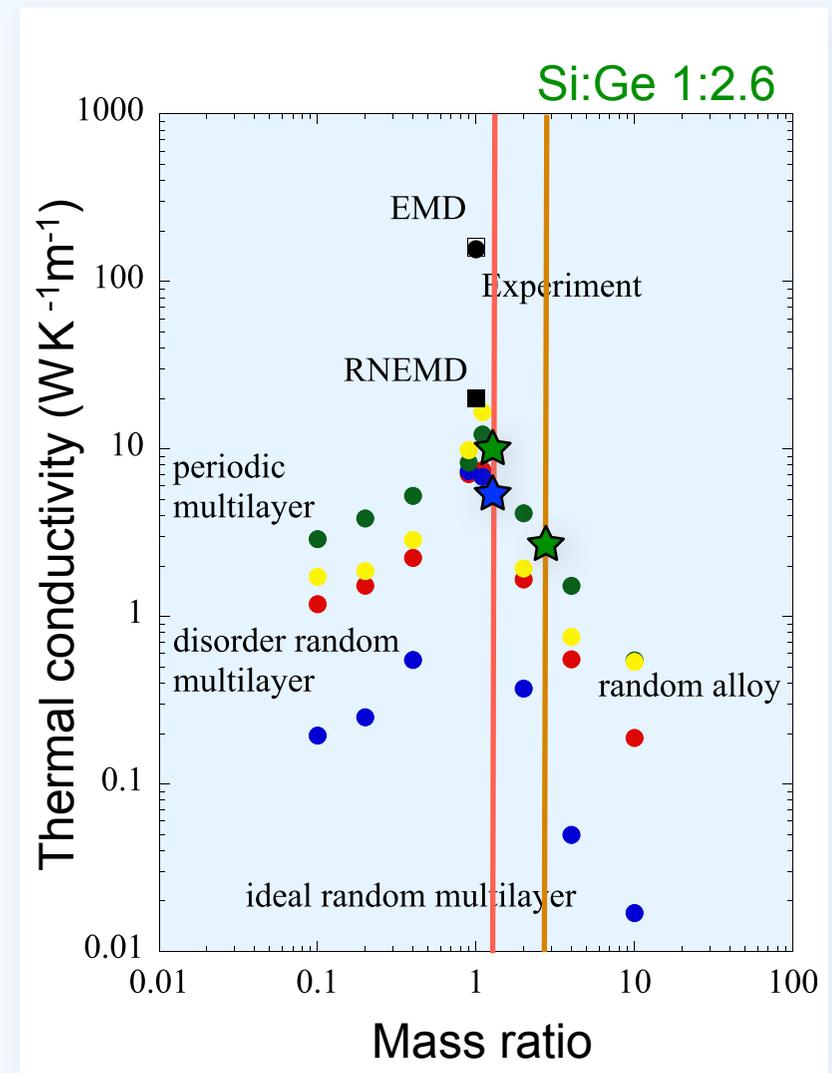
Defect issues



[Watling, Paul: J Appl Phys **110** (2011) 114508]

Conclusions

- ◆ Lowest κ_{\perp} for SL with highest Ge content
- ◆ κ_{\perp} a function of the SL period
[cf. e.g. Rawat *et al*: J Appl Phys 105 (2009) 024909]
- ◆ Only a small reduction in κ_{\perp} for random multilayers[★] compared to SL[★] observed due to low mass ratio in the multilayers investigated so far
 - With higher Ge content,
0.1 $\text{WK}^{-1}\text{m}^{-1}$ may be expected !
- ◆ Random multilayers exhibit a decrease in κ_{\parallel} by $\approx 50\%$



[Frachioni, White:
J Appl Phys **112** (2012) 14320]

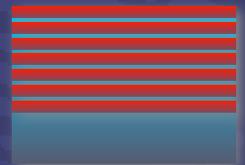
Acknowledgments

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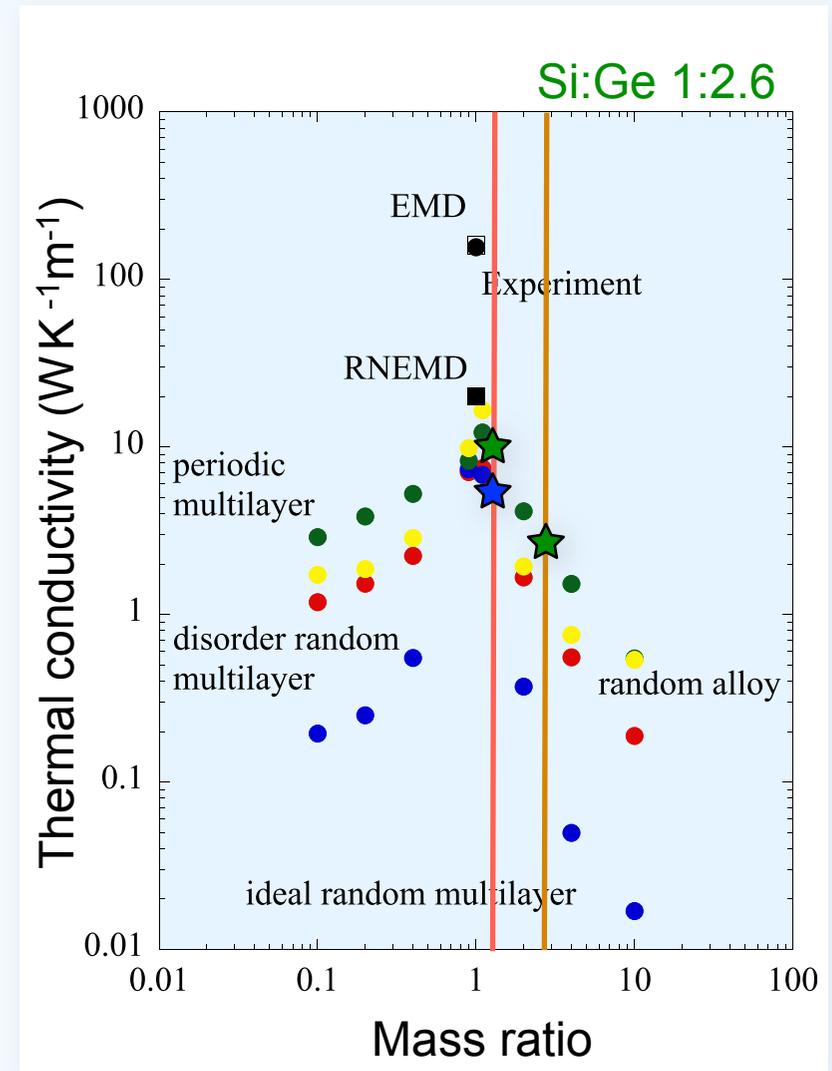
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References

- ◆ Frachioni, White: J Appl Phys **112** (2012) 14320.
- ◆ Tonkikh *et al*/ Thin Sol Films (2011) doi: [10.1016/j.tsf.2011.10.049](https://doi.org/10.1016/j.tsf.2011.10.049).
- ◆ Watling, Paul: J Appl Phys **110** (2011) 114508.
- ◆ Rawat *et al*: J Appl Phys **105** (2009) 024909.